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Instability of dilative sand

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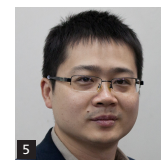
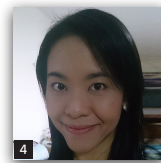
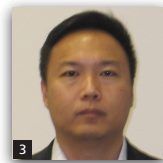
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A type of pre-failure instability that occurs for medium loose to dense sand under fully drained conditions is studied in this paper. It is observed experimentally that when a specimen is sheared along a drained stress path involving a decrease in the effective mean stress, it becomes unstable after the stress path crosses an instability line (IL). The IL specifies a minimum stress ratio under which instability may occur. It is not unique but changes with the void ratio of the soil and the applied effective stresses. The instability occurring under drained conditions is different from that under undrained conditions. The differences and similarities between the two types of instability are pointed out. Practical implications of the study in analysing the failure mechanisms of granular soil slopes under various drainage conditions are discussed.

Notation

$d\varepsilon_1/dt$	axial strain rate
$d\varepsilon_v/d\varepsilon_1$	strain increment ratio
$(d\varepsilon_v/d\varepsilon_1)_i$	$d\varepsilon_v/d\varepsilon_1$ imposed to specimen
$(d\varepsilon_v/d\varepsilon_1)_s$	the maximum $d\varepsilon_v/d\varepsilon_1$ obtained in a drained test
e	void ratio
e_c	e at the end of consolidation
e_{cr}	e at critical state
e_d	e at the end of drained shearing
e_f	e at failure
e_{IL}	e at the onset of instability
M	effective stress ratio ($= q/p'$)
M_{cs}	slope of critical state line
M_f	slope of failure line
M_{IL}	slope of instability line
M_L	slope of constant stress ratio line
p'	mean effective stress ($=(\sigma'_1 + 2\sigma'_3)/3$)
q	deviator stress ($=(\sigma_1 - \sigma_3)$)
ε_1	axial strain
ε_v	volumetric strain (compression positive)
σ'_1	effective major principal stress
σ'_3	effective minor principal stress
ψ	state parameter ($= e - e_{cr}$)

Introduction

Failure of geotechnical structures can be initiated by instability of soil. The term instability as used in this paper refers to a behaviour in which large plastic strains are generated rapidly due to the inability of a soil element to sustain a given load or stress. Instability is normally considered to have taken place when the stress state of a soil element satisfies a failure criterion, as in the conventional stability analysis. Instability may also occur prior to attaining the failure stress state. A typical example is static liquefaction, which occurs before the effective stress path reaches the failure line (FL) or the steady state line (SSL). So far, this so-called pre-failure instability has been studied mainly for saturated loose sand under undrained conditions (e.g. Andrade, 2009; Bobei *et al.*, 2009; Chu and Wanatowski, 2008; Daouadji *et al.*, 2010; di Prisco and Imposimato, 1997; Gajo *et al.*, 2000; Ishihara, 1993; Lade, 1992; Lade and Pradel, 1990; Lade and Yamamuro, 2011; Lade *et al.*, 1987, 1988; Leong *et al.*, 2000; Monkul *et al.*, 2011; Sawicki and Swidzinski, 2010; Seed, 1987; Wanatowski and Chu, 2007, 2012; Zhao and Zhang, 2014). However, there are several cases in which failure occurs under drained rather than undrained conditions. Using a fully instrumented model slope of a loose granular material, Eckersley (1990) observed that the failure in his model tests was initiated under essentially static, drained conditions, and the pore

water pressure increases in his model tests were only a consequence of the failure. In all his model tests, flow slides occurred in slopes that were gentler than the angle of repose of the sand. In re-analysis of the failure of the north dike of Wachusett dam, Olson *et al.* (2000) concluded static liquefaction under a completely drained condition to be the likely failure mechanism. Therefore, there is a need to investigate the instability mechanisms of sand under drained conditions.

Although flow slide and liquefaction have been observed to occur mainly in relatively loose or contractive sand, there are cases where failure occurs in relatively dense or dilative sand. The first such case was mentioned by Casagrande (1975). He described a natural phenomenon, which in the European Alps is known by the name Muren, in which large masses of dense granular talus liquefy and flow down a valley and suggested that dilation of soil was involved in the failure process. Several other cases were reported by Been *et al.* (1988), Fleming *et al.* (1989) and Terzaghi (1957). Been *et al.* (1987) also argued that the Nerlerk berm failure case (Lade, 1993; Sladen *et al.*, 1985) might have occurred for dilative sand, which lies below the SSL. Based on field observations, Fleming *et al.* (1989) have classified flow failure into two categories: the contractive and dilative flow slides. A well-documented case where flow slide occurred in dense sand was the Mississippi riverbank failure presented by Hadala and Torrey (1989) and Torrey and Weaver (1984). It has been concluded unambiguously by Hadala and Torrey (1989) and Schofield (1980) that the failure in the above case was not caused by static liquefaction or instability under undrained conditions, and this is confirmed by the laboratory tests. Although some explanations as to the causes of failure have been proposed (Hadala and Torrey, 1989; Schofield, 1980; Torrey and Weaver, 1984), the instability mechanisms of dilative sand have not been well established.

More recently, further studies on instability for different soils and different conditions were carried out. A topic that has drawn interest is the influence of fines on the instability and static liquefaction of sands (Lade and Yamamuro, 2011; Rahman and Lo, 2014; Rahman *et al.*, 2014; Zhao and Zhang, 2014). Compared with clean sand, sands with fines or silts are more compressible, which leads to a liability to pre-failure instability and static liquefaction (Bobei *et al.*, 2009; Lade and Yamamuro, 2011; Rahman and Lo, 2014; Rahman *et al.*, 2014). Instability for unsaturated soil also received research interest (Buscarnera and Nova, 2011; Farooq *et al.*, 2004; Zhao and Zhang, 2014). It was found that the instability of unsaturated soil along wetting path depends on the stress ratio and net confining pressure. Instability in an unsaturated sand occurs at higher suction when it is subjected to a higher stress ratio or a higher net confining pressure (Zhao and Zhang, 2014). Experimental studies on the instability of soil were also carried out under a water seepage condition, which can simulate the water infiltration into soil slopes (Lourenço *et al.*, 2011). The constant shear drained (CSD) tests on soil specimens with increasing pore pressure in the upstream and free drainage in the downstream show pre-failure instability in the form of a rapid increase in axial strain before reaching the critical state line (CSL; Lourenço *et al.*, 2011).

It should also be pointed out that numerical modelling of soil instability incorporating Hill's instability criterion (Hill, 1958) has been carried out by several research teams to capture the phenomenon of soil instability (Andrade, 2009; Buscarnera and Whittle, 2013; Lignon *et al.*, 2009). Other numerical tools, especially discrete element methods (e.g. Nicot *et al.*, 2011), were also adopted to explain the mechanism of pre-failure instability of granular materials. However, full understanding of pre-failure instability and, in particular, the ability to predict its occurrence, has not yet been achieved.

Slope failures are often caused not only by an increase in external load but also by a reduction in the effective mean stress, which is due to, for example, water infiltration into slopes (Leroueil, 2001; Zhu and Anderson, 1998). The Aberfan coal tip disaster in the UK, which killed 144 people (Bishop, 1973), is one of the examples. As suggested by Brand (1981), when investigating the failure mechanisms of slopes, the stress-strain behaviour of the soil along stress paths that simulate water infiltration should be studied. Such stress paths may be idealised as paths with constant shear stress, but decreasing mean effective stress, or the so-called constant shear-drained (CSD) tests performed under constant deviator stress (Anderson and Riemer, 1995; Anderson and Sitar, 1995; Brand, 1981; Zhu and Anderson, 1998). The instability behaviour of contractive sand along the CSD stress paths has been studied by several researchers (Anderson and Riemer, 1995; Chu *et al.*, 2003; Daouadji *et al.*, 2010; Darve *et al.*, 2004, 2007; Orense *et al.*, 2004; Wanatowski *et al.*, 2010; Zhu and Anderson, 1998). However, only a few studies have been carried out to investigate how dilative sand responds to this type of stress paths (Chu *et al.*, 2003; Darve *et al.*, 2004; Wanatowski *et al.*, 2010). There are also failure cases of dilative slopes that occurred under other than fully drained conditions (Adalier and Elgamal, 2002; Been *et al.*, 1988; Fleming *et al.*, 1989; Kokusho, 2003; Sento *et al.*, 2004). These failure types cannot be simulated under fully drained or undrained conditions.

The objectives of this paper are to emphasise that dilative sand can become unstable under drainage conditions in which water infiltrates into the soil mass and to discuss the most important factors that govern the instability of dilative sand.

Material tested

A marine-dredged sand was used for this experimental study. The sand was used for land reclamation of the Changi International Airport in Singapore. It was dug out from the seabed on the central eastern coast of Sumatra Island, administrated by Riau and Bangka-Belitung provinces of Indonesia, both adjacent to Singapore. The grain size distribution curve of the sand is shown in Figure 1. The basic properties of the sand are given in Table 1. The loose specimens were prepared by a moist tamping method in which the sand was pre-mixed to a moisture content of 5% and was saturated after the formation of the specimen. The dense specimens were prepared by pluviating sand into water. The nominal dimension of the specimen was 100 mm in diameter and 200 mm in height. A

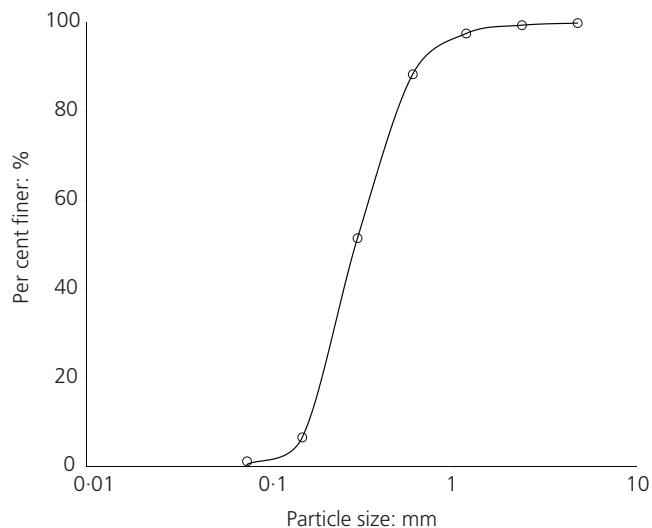


Figure 1. Grain size distribution curve of Changi sand

	DR39	DR40	ISTD08	ISTD09
After consolidation				
e_c	0.657	0.647	0.668	0.663
q/p'	0	0	0	0
σ_3' : kPa	150	150	100	200
Before reduction of cell pressure				
e_d	0.654	0.644	0.664	0.660
q/p'	1.21	1.31	0.97	0.57
σ_3' : kPa	149	148	98	198
At the onset of instability				
e_{IL}	0.659	0.649	0.695	0.708
q/p'	1.64	1.66	1.40	1.40
σ_3' : kPa	83	91	61	61

Table 2. Test conditions at different stages for dense specimens sheared along the CSD path

summary of the drained instability tests presented and discussed in this paper is given in Table 2.

Testing arrangement

The experiments were carried out using a fully automated triaxial testing system as illustrated in Figure 2. A digital pressure volume controller (DPVC) with a remote feedback module was used to control the axial load by way of a hydraulic actuator. Another DPVC was used to control the confining stress. A third DPVC was used to control the back pressure by way of the base of the specimen and measure the volume change at the same time. The pore water pressure at the top of the specimen was measured by a pressure transducer. For the details of the testing arrangement, see the works of Leong *et al.* (2000) and Chu and Leong (2001).

Results

Instability line and instability under undrained conditions

Firstly, the results of some isotropically consolidated drained (CD) and undrained (CU) tests on loose sand are presented in Figure 3(a) to define the FL and the instability line (IL). The FL determined for

loose sand is the same as the CSL or the SSL (Chu, 1995; Leong *et al.*, 2000; Wanatowski and Chu, 2007). The IL is defined by the peak points of the effective stress paths of the undrained tests (Lade, 1992, 1993). The zone in between the FL and IL defines the zone of potential instability. It is known that that the IL is not unique but is affected by the void ratio of the soil, as shown in Figure 3(b). The IL is also affected by the effective confining stress. However, within a limited stress range, a linear IL can be defined as shown in Figure 3(a). The slope of the IL will be denoted as M_{IL} in this paper.

When sand is dilative, that is, when the void ratio of sand is smaller than the void ratio at critical state, the specimen becomes dilative and a peak is no longer obtainable. In this case, the effective stress path in an undrained test will increase monotonically and approach a constant stress ratio line (CSRL) as shown in Figure 4. Chu *et al.* (2003) showed that a yield surface determined by CD tests on dense sand coincides with the CSRL obtained from the CU tests. Therefore, the CSRL can be used to determine the yield surface for dense sand. Chu *et al.* (2003) also reported that the CSRL is not sensitive to void ratio change, although generally the denser the soil, the higher the CSRL (Loke, 2004). Similar results were also reported by Chu and Lo (1993, 1994), Mooney *et al.* (1998), Tsukamoto *et al.* (1998) and Wanatowski *et al.* (2010). The CSL and

Type	Mean size: mm	Uniformity coefficient	Specific gravity	Maximum void ratio	Minimum void ratio	Fines content: %	Shell content: %
Marine dredged sand	0.3–0.35	2.0	2.60	0.916	0.533	0.4	14

Table 1. Basic properties of the tested sand

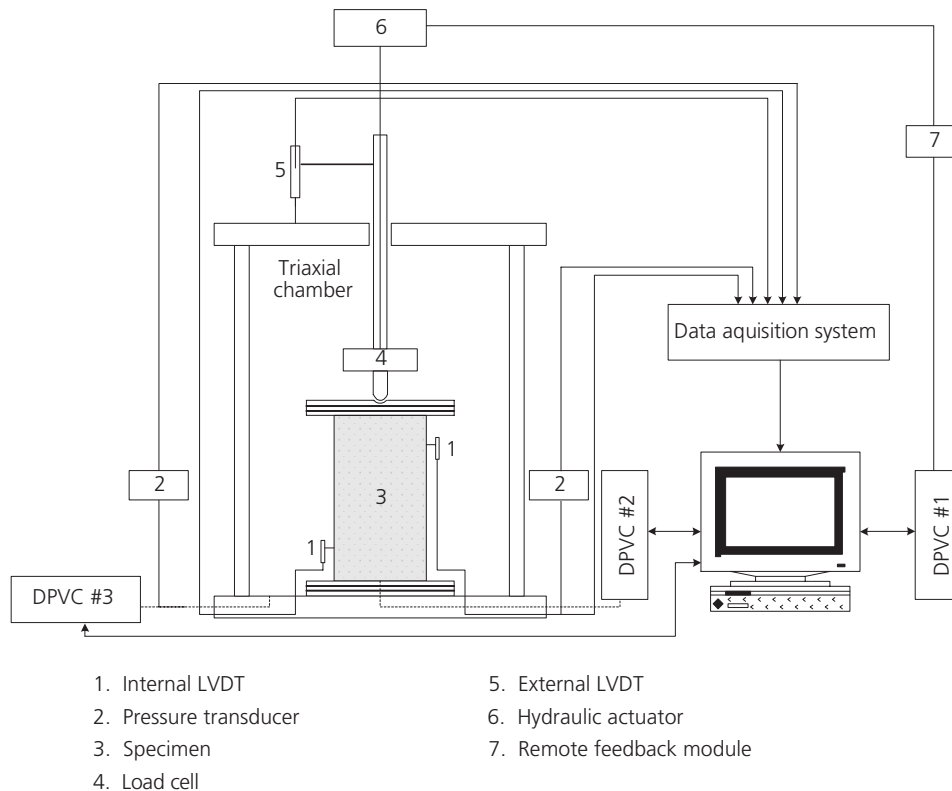


Figure 2. Testing arrangement

the FL obtained from CD tests on specimens with comparable void ratios are also shown in Figure 4. It can be seen that the CSRL lies in between the FL and the CSL. The slopes of the FL and the CSRL obtained from Figure 4 are $M_f = 1.63$ and $M_L = 1.5$, respectively.

Based on Figures 3(b) and 4 and other similar test results, the slope of each IL, M_{IL} , is plotted in Figure 5 against $e - e_{cr}$, where e is the void ratio at the instability point, and e_{cr} is the void ratio at the critical state at the same effective mean stress. It can be seen that the M_{IL} levels off when the soil becomes extremely dense or loose.

Instability of contractive sand under drained conditions

It has been shown by several researchers that a loose sand specimen will become unstable under an undrained condition when the stress state applied to the specimen is within the zone of instability (Chu *et al.*, 2003; Darve *et al.*, 2004; Lade, 1992; Leong *et al.*, 2000; Sasitharan *et al.*, 1993). An example for the tested soil is shown in the work of Chu *et al.* (2003). A loose sand specimen can also become unstable under drained conditions when the specimen is sheared along a CSD path. This has been discussed in detail in the work of Chu *et al.* (2003). The test results are summarised in Figure 6. The stress ratio at which the specimen becomes unstable, M_{IL} , increases with the decrease in void ratio. For more information on Figure 6, see the work of Chu *et al.* (2003).

Instability of dilative sand under drained conditions

Two tests, DR39 and DR40, were conducted on sand specimens with the consolidated void ratios of 0.657 and 0.647, respectively. The effective stress paths followed in the two tests are presented in Figure 7. After isotropic consolidation, the specimens were firstly sheared drained to points A (for DR39) or A' (for DR40). Starting from point A (or A'), a CSD path was imposed with the mean stress reduced while the deviator stress was kept constant under a fully drained condition. The axial and volumetric strains plotted against time and the axial and volumetric strains plotted against mean effective stress curves are shown in Figures 8 and 9 for tests DR39 and DR40, respectively. It can be seen from Figures 8(a) and 9(a) that the axial strain started to increase abruptly at points B and B' for tests DR39 and DR40, respectively, signifying the onset of instability. The volumetric strain, ϵ_v , also began to develop rapidly at point B (or B'), respectively. It should be noted that the volumetric strain was in dilation. This observation is different from that for loose sand where the volumetric change is in compression (Chu *et al.*, 2003).

To examine the stress state at point B (or B') where instability starts to develop, the CSL, the CSRL and the FL are plotted in Figure 7. The FL is drawn as the envelope to the two stress paths. As instability started at point B (or B'), the line passing through point B (or B') defines the IL, which coincides with the CSRL (see

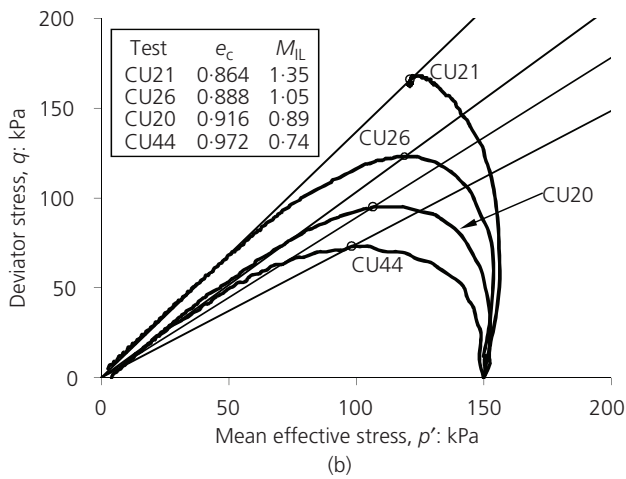
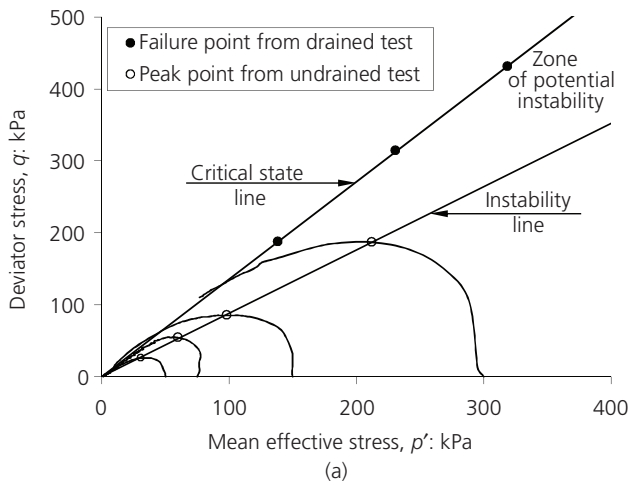


Figure 3. The instability line defined by undrained tests: (a) instability line and zone of potential instability; (b) dependence of instability line on the void ratio of sand

Figure 7). The slope of this IL is higher than that of the CSL but lower than that of the FL. It can also be seen from Figures 8(b) and 9(b) that large yielding starts to develop at points B and B'. Therefore, points B and B' are also two yield points for tests DR39 and DR40, respectively. This explains why the IL and the CSRL are the same for these two tests.

Another two CSD tests, ISTD08 and ISTD09, are conducted on specimens with consolidated void ratios of 0.668 and 0.663, respectively (Figure 10). As shown in Figure 10(a), the two tests are conducted along the same CSD path, but starting from two different initial stress states (points A and A'). The axial strain and volumetric strain plotted against time curves are shown in Figures 10(b) and 10(c) for the two tests, respectively, from which the onset of instability points can be determined as points B and B'. It can be seen from Figure 10(a) that points B and B' are almost the same. Using these points, the IL can be defined as shown in Figure 10(a). The IL is located above the CSL but below the FL.

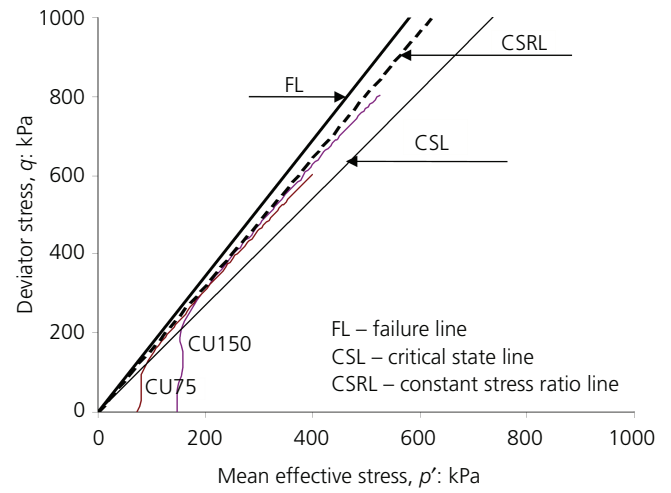


Figure 4. Effective stress paths of undrained tests on medium dense sand

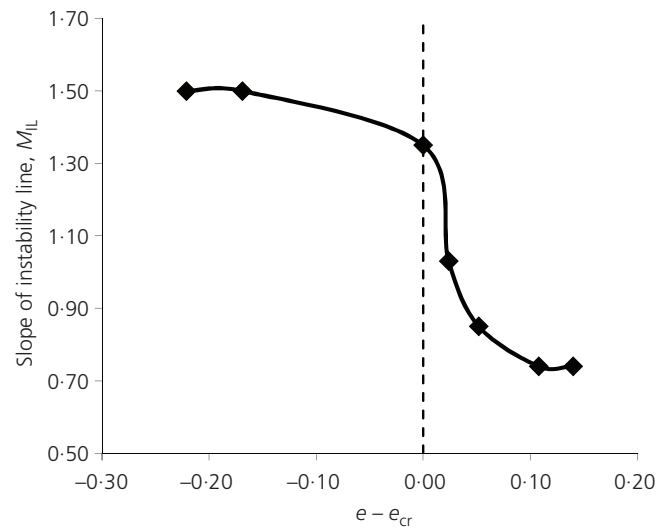


Figure 5. Relationship between the slope of the instability line, M_{IL} , and $e - e_{cr}$

Discussion

Physical meaning

Instability as defined in this paper refers to behaviour in which large plastic strains are generated rapidly. For large plastic strain to develop, the soil must be in a yielding state. Therefore, yielding is the necessary condition for instability. This has been explained by Lade (1992) for the instability occurring for loose sand under undrained conditions. The IL, in fact, is associated with the yield surface and defines the conditions in which plastic yielding can take place (Chu *et al.*, 1993, 2003; Imam *et al.*, 2002; Lade, 1992; Wanatowski *et al.*, 2010). As such, the zone of instability is defined without specifying the drainage condition. In fact, the instability

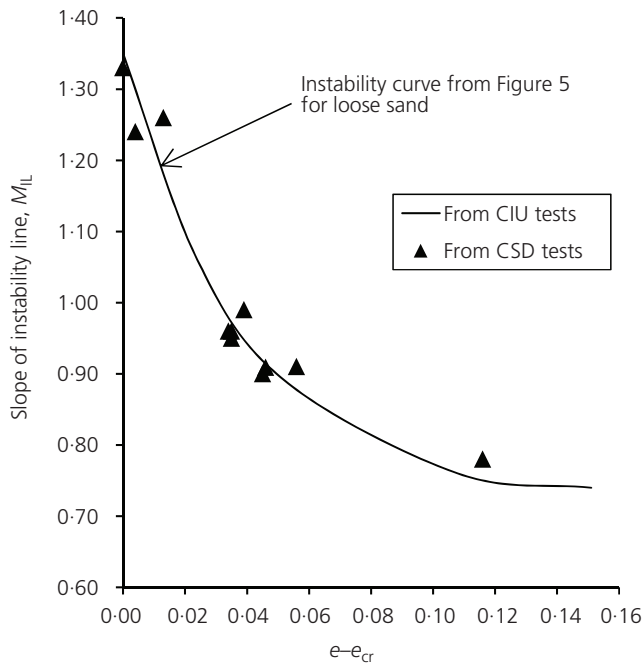


Figure 6. Comparison of the $M_{IL}-(e-e_{cr})$ relationship obtained from CSD tests and the instability curve defined in Figure 5 for loose sand

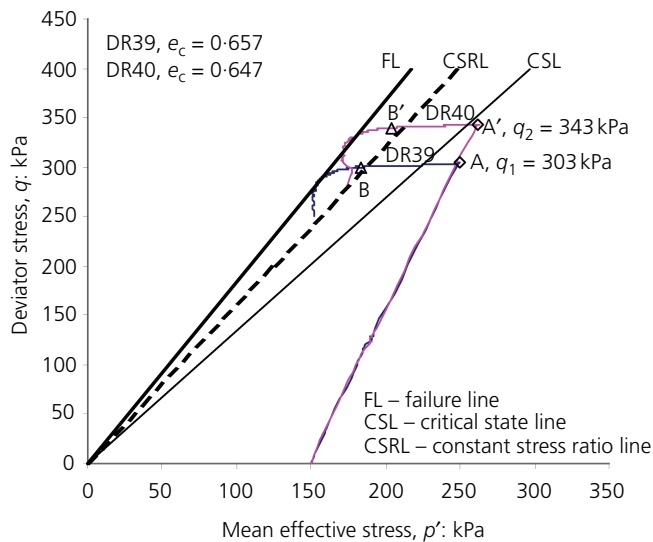


Figure 7. Effective stress paths of tests DR39 and DR40

conditions of loose sand occurring under both undrained and drained conditions are defined by the same zone of instability, as shown in Figure 6 and discussed in detail by Chu *et al.* (2003) and Wanatowski *et al.* (2010).

As mentioned in the Introduction, instability will not occur under undrained conditions for dilative sand. This is because when a

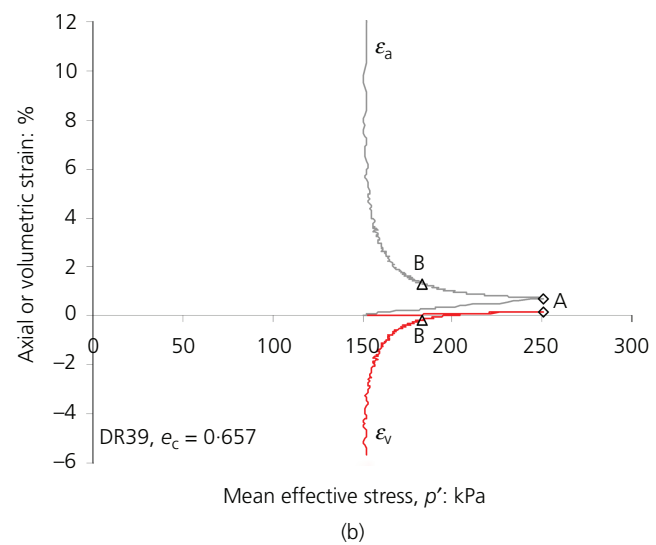
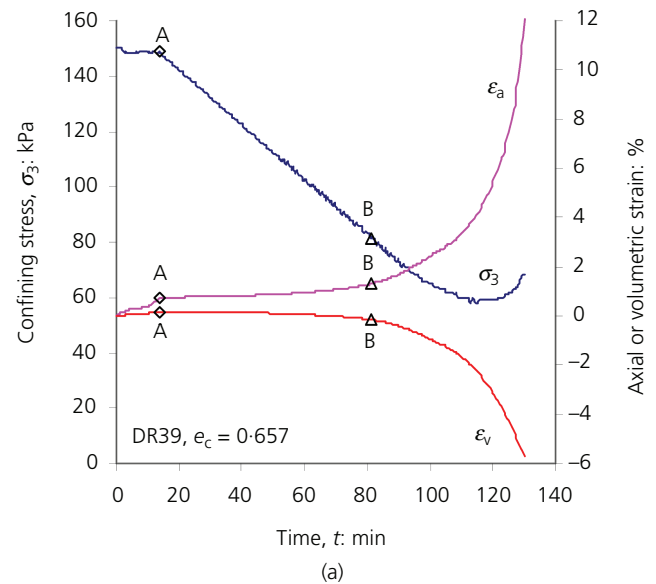


Figure 8. Results of test DR39: (a) variation of axial and volumetric strains with time curves; (b) axial and volumetric strains versus mean effective stress curve

dilative specimen is sheared under an undrained condition with the deviator load maintained constant, the pore water pressure will be reduced and the resulting effective stress moves inside the yield surface and thus a sustained plastic strain will not be generated.

When a dilative specimen is sheared under a drained condition along a CSD path, the effective stress path moves toward the FL. Once the stress path crosses the IL, that is, cuts the yield surface, plastic strain will be generated. Therefore, the instability that occurred for dilative specimens along the CSD path is also associated with plastic yielding. This explains why in tests DR39 and DR40, the onset of instability points, B and B', are also the yield points as can be seen from Figures 8(b) and 9(b) for tests DR39 and DR40,

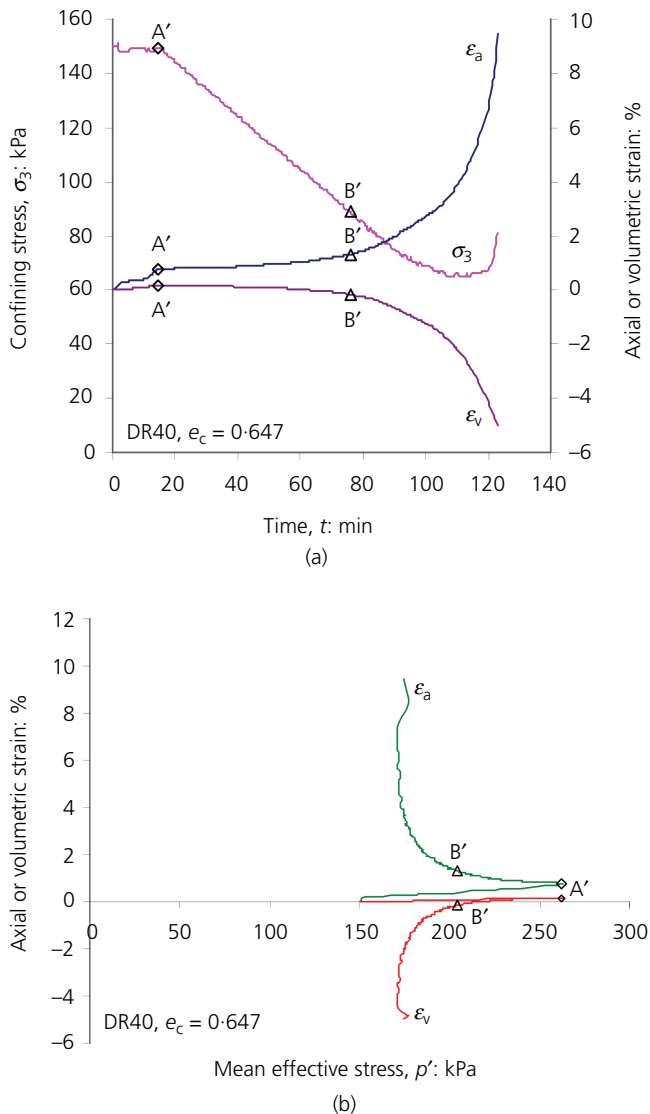


Figure 9. Results of test DR40: (a) variation of axial and volumetric strains with time curves; (b) axial and volumetric strains versus mean effective stress curve

respectively. For dense sand, the yielding condition appears to be defined by the CSRL, which assembles the yield surface, as shown in Figure 4. Therefore, the CSRL defines the stress ratio at which dilation and the associated large plastic yielding will start to develop. This explains why the onset of instability points B and B' coincides with the CSRL.

Although yielding is the necessary condition for instability to occur, it is not sufficient. In other words, plastic yielding does not necessarily cause a soil specimen to be unstable. Yielding means the development of a large strain for a small change in stress. It does not imply that the specimen will become unstable, which is characterised by a sudden increase in the strain increment rate, $d\epsilon_i/dt$. Therefore, it cannot be assumed that yielding is automatically

the condition for instability. Whether instability can occur along a given stress path needs to be established separately.

Instability lines

The effective stress paths of the four instability tests DR39, DR40, ISTD08 and ISTD09 are presented in Figure 11 together with the CSL, the FLs and the ILs. It can be seen from Figure 11 that for dilative sand, the ILs are all above the CSL and the slope of the IL increases with the decrease in the void ratio of sand. It should be noted that the slope of the FL is not fixed but increases with the decrease in the void ratio, as the friction angle of dilative sand is dependent on the void ratio.

Combining the data obtained from instability tests on both contractive (Chu *et al.*, 2003) and dilative sand, a relationship between the stress ratios of the ILs and the void ratios of soil at the onset of instability can be established in Figure 12. All the tests were conducted under the same effective confining stress (150 kPa), except ISTD08 and ISTD09. By connecting these points (shown by squares), an instability curve representing the change of the slope of IL with the void ratio at instability (e_{IL}) can be obtained, as shown in Figure 12. The void ratio and the effective stress ratio at the onset of conditional instability obtained from all the CSD instability tests are also plotted in Figure 12 as points for comparison. The data for loose to medium loose and medium dense to dense specimens are marked differently by diamonds (i.e. loose) and triangles (i.e. dense) in Figure 12. It can be seen from Figure 12 that a rather good agreement between the instability points and the instability curve is achieved, particularly for the dilative sand. It proves that the CSRL can be used to define the IL for dilative sand.

As shown in Figure 12, the instability conditions defined for soils with void ratios greater or smaller than the void ratio at the critical state are quite different. The slope of the IL, M_{IL} , decreases abruptly when the void ratio becomes slightly greater than the void ratio at the critical state. On the other hand, when the void ratio is getting smaller than the void ratio at the critical state, M_{IL} only increases marginally. This is consistent with the experimental observation that for medium loose to medium dense sand, the CSRL does not seem to change much with the void ratio (Mooney *et al.*, 1998; Tsukamoto *et al.*, 1998), although generally speaking, the slope of the CSRL should increase with the decrease in the void ratio. It should also be pointed out that within a certain stress range, the stress ratio of the CSRL is not affected by the initial stress state and the stress history prior to an undrained path, as established by Chu and Lo (1994) and Kato *et al.* (2001). It can also be seen from Figure 12 that the instability curve seems to approach asymptotically some limiting q/p' values when the sand becomes very loose or very dense. From the data available, q/p' at instability would be approximately constant and equal to 0.8 for $e > 0.95$ and 1.50 for $e < 0.7$.

Differences in instability for contractive and dilative sand

Although instability is observed to occur for both contractive (or loose) and dilative (or dense) sand, the types of instability can be

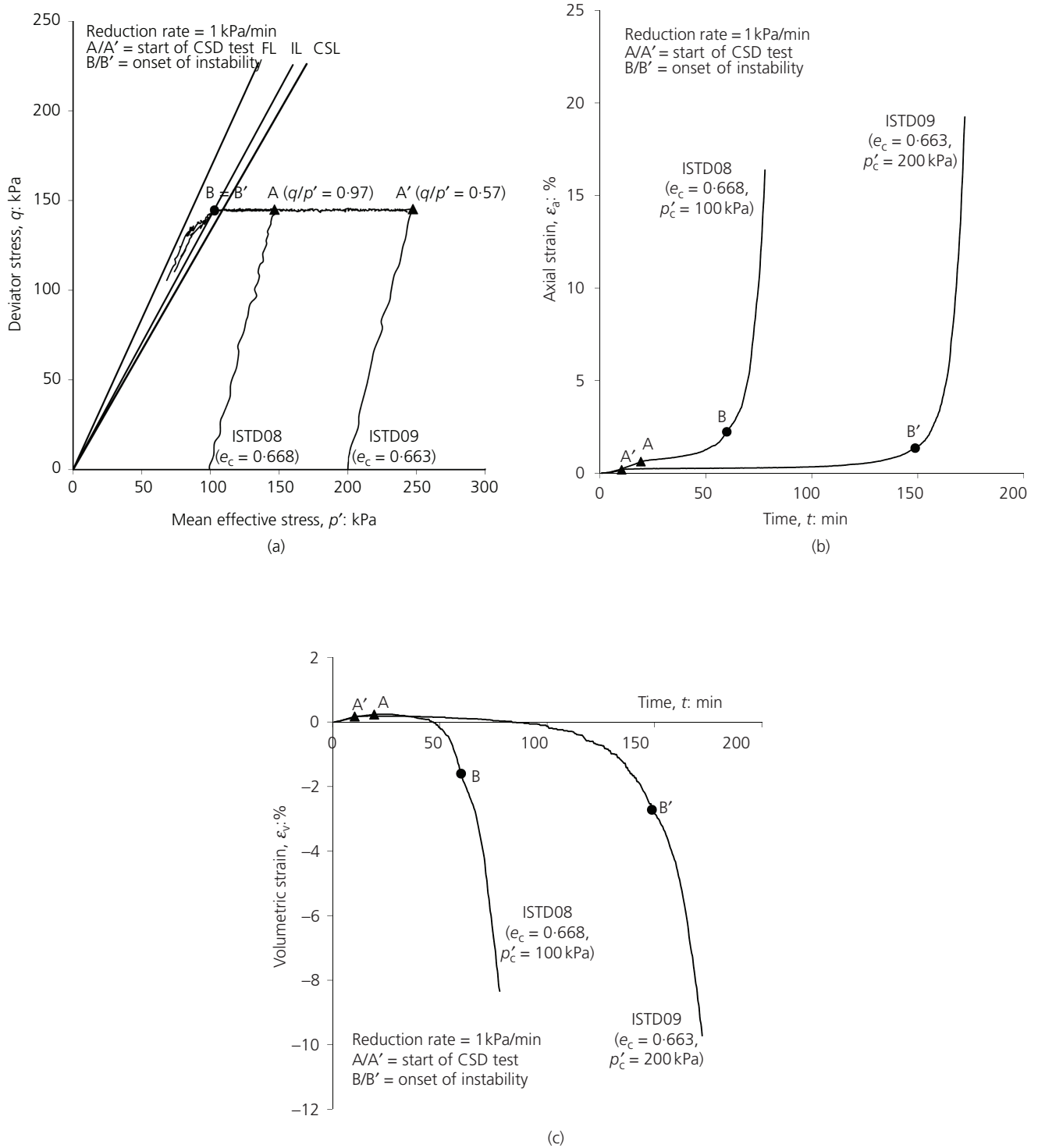


Figure 10. Results of tests ISTD08 and ISTD09: (a) effective stress paths; (b) change in axial strain with time; (c) change in volumetric strain with time

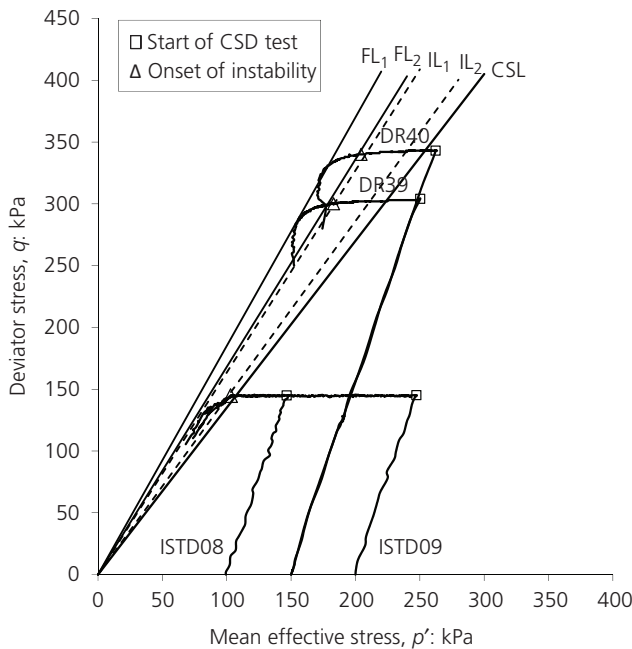


Figure 11. Summary of drained instability tests on dense sand on the $q-p'$ plane

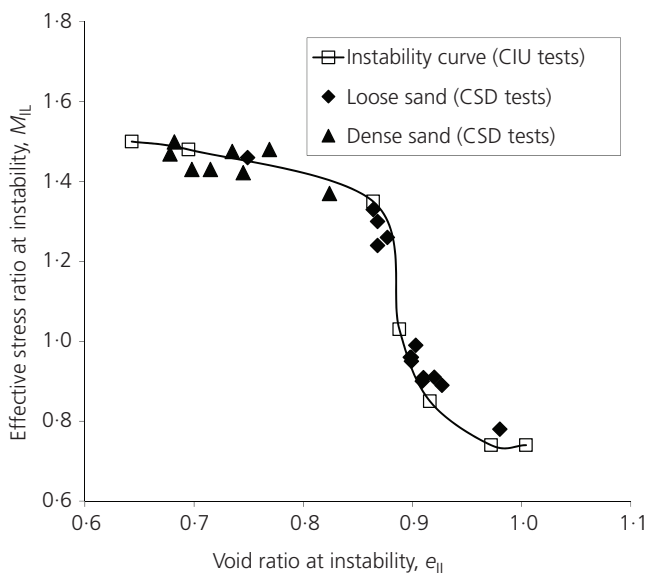


Figure 12. Relationship between the stress ratio at instability and the void ratio of soil

different. First, for contractive sand, instability can occur under either drained or undrained conditions, whereas for dilative sand, instability cannot occur under undrained conditions. It needs to be pointed out that the undrained instability is different from the drained instability, as discussed in detail by Chu *et al.* (2003). The instability that occurs under undrained conditions is a runaway type because once runaway instability is initiated, the pore water pressure

and the axial strain rates increase dramatically and the soil specimen collapses almost instantly. In other words, the runaway instability cannot be stopped (Chu *et al.*, 2003; Wanatowski and Chu, 2012). The instability under drained conditions is not a runaway type and has been called conditional instability by Chu *et al.* (2003). This is because the soil specimen does not collapse instantly during a drained instability test. Furthermore, instability under drained conditions can only take place along a stress path with a reduction in the mean effective stress. Therefore, for dilative sand, only conditional instability will occur under drained conditions, and this type of instability is different from the runaway type of instability occurring for contractive sand, for example, static liquefaction behaviour. Therefore, contractive sand can become unstable, but it does not imply that dense sand can liquefy as loose sand. The term ‘instability’ as defined in this paper carries a broader meaning than liquefaction or collapse of soil. In addition to runaway type of failure, the conditions where strain increases suddenly at an accelerating rate should also be established and considered in stability analysis.

Because the conditions for both types of instability are the same for loose sand, when a conditional instability occurs under a drained condition, it may evolve into a runaway instability if the drainage is insufficient to dissipate all the pore water pressure, for example, during an earthquake. This was observed in some of the tests. The drained collapse behaviour reported by Sasitharan *et al.* (1993) may belong to this type, in which ‘a slight increase in pore water (6.7 kPa) followed by a catastrophic undrained failure or collapse of the sample’ was observed. Similar observations were made by Eckersley (1990) from his model tests. He reported that static liquefaction had occurred for loose sand under essentially static, drained conditions (Eckersley, 1990). The flow slides in Eckersley’s experiments were initiated by slow water level increases, that is, along a stress path with a reduction in effective mean stress. Therefore, the flow slides in these model tests are likely caused by drained instability. Eckersley (1990) also reported that excess pore water pressures were developed after the start of flow slides. This pore water pressure building up was likely caused by the inability to dissipate fully the pore water, which was generated as a result of large volumetric strain development. The drained instability also offers an explanation for the failure of the north dike of Wachusett dam, where the failure is considered to occur under a completely drained condition (Olson *et al.*, 2000).

It can also be explained now why under drained conditions instability was not observed in the tests reported by Lade *et al.* (1987), Chu (1991), and Leong *et al.* (2000). That is because those tests were conducted under a fixed stress state rather than along a stress path with reduction in the effective mean stress (i.e. the CSD path).

Other drainage conditions

It has been explained in previous sections that dilative sand does not become unstable under undrained conditions, but it may become unstable under fully drained conditions. It needs to be emphasised, however, that there are failure cases of dilative sand that occurred under other than fully drained conditions (e.g. Adalier and Elgamil, 2002; Sento *et al.*, 2004; Torrey and Weaver, 1984). The possibility

of dilating behaviour of soil masses prior to slope collapse has been reported in several case studies. For example, Been *et al.* (1987) argued that the Nerlerk berm failure case might have occurred for dilatant sand, which state lies below the SSL. Several other cases of flowslide in dilatant sand have been presented by Been *et al.* (1988). Fleming *et al.* (1989) also reported that the Salmon Creek landslide in Marin Country, California, exhibited dominantly dilative transformation from solid landslide to liquid debris flow. Although some explanations for the causes of this and other failures have been proposed (Been *et al.*, 1988; Hadala and Torrey, 1989; Schofield, 1980), the instability mechanisms of dilative sand have not been fully explained.

When dilative sand in a slope is subjected to conditions in which pore water pressure and volume of soil mass can change simultaneously, pre-failure instability can become possible, even though drainage conditions in such cases are neither completely undrained nor fully drained. These drainage conditions can be simulated experimentally by strain paths with the strain increment ratio ($d\epsilon_v/d\epsilon_1$) precisely controlled (Chu, 1991; Chu and Leong, 2001; Chu *et al.*, 1993, 2015; Lancelot *et al.*, 2004; Sivathayalan and Logeswaran, 2007; Vaid and Eliadorani, 1998; Wanatowski and Chu, 2011; Wanatowski *et al.*, 2008). When $d\epsilon_v/d\epsilon_1 > 0$ is imposed on dense sand, the pore water pressure will reduce and instability will not occur. However, when an adequate dilative $d\epsilon_v/d\epsilon_1$ is imposed, the pore water pressure will increase and instability becomes a possibility.

An example of instability test IST01, conducted on medium dense (i.e. dilative) sand, in order to illustrate that pre-failure instability can occur under dilatancy rate-controlled conditions, is shown in Figure 13.

The effective stress path obtained from test IST01 is plotted in Figure 13(a). The CSL and the FL obtained from drained triaxial tests on loose and dense Changi sand are also shown in Figure 13(a). The slopes of the CSL and the FL are $M_{cs} = 1.35$ and $M_f = 1.63$, respectively (Chu *et al.*, 2003; Wanatowski and Chu, 2007). As shown in Figure 13(a), the specimen in test IST01 was first sheared along a drained path from $p'_c = 150$ kPa to a stress ratio of $q/p' = 1.13$. After that, the external loads, that is, the axial load and the cell pressure, were maintained constant to conduct an instability check along a strain path of $d\epsilon_v/d\epsilon_1 = -0.67$. Under these conditions, instability occurred at point B, and the axial strain and the pore water pressure increased suddenly, as shown in Figure 13(b). After occurrence of such instability, it was no longer possible to maintain the axial load constant, and thus the deviatoric stress dropped significantly, as can be seen in Figure 13(a). Physically, it was observed that the specimen collapsed suddenly, that is, pre-failure instability had occurred. This behaviour resembles the instability that occurs in loose sand under undrained conditions. This observation shows that dense sand, despite exhibiting strain hardening behaviour under an undrained condition, can become as vulnerable as loose sand when it is subjected to a dilative strain path.

It needs to be pointed out that the instability shown in Figure 13 was not only due to the control of a negative strain increment ratio but

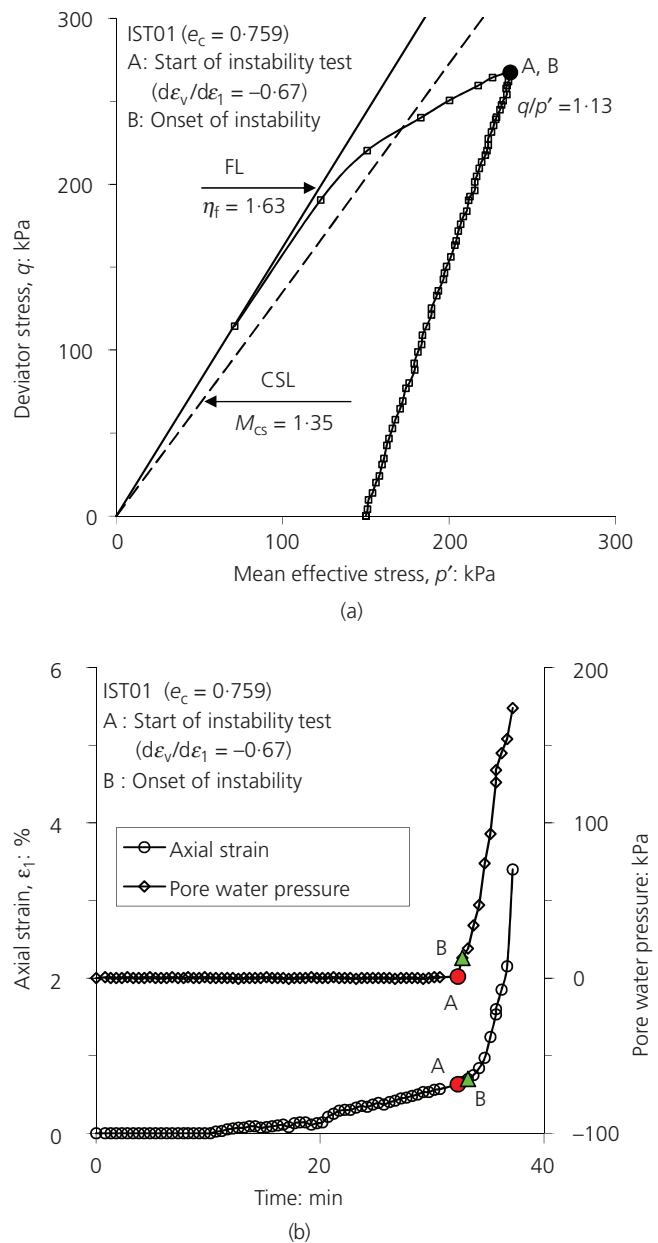


Figure 13. Pre-failure instability of dilative sand under dilatancy rate-controlled conditions: (a) effective stress path; (b) axial strain and excess pore water pressure versus time curves

also due to the stress state upon the instability check, as reported by Chu *et al.* (1993) and Chu and Leong (2001). Furthermore, the observed instability was not due to strain localization or rate/time effect, as explained by Chu *et al.* (1993) and Wanatowski and Chu (2011). This type of pre-failure instability can only occur when appropriate conditions are met (i.e. adequate strain increment ratio and stress state).

It is well known that when sand of different void ratios is sheared under a drained condition, the volumetric strain behaviour will

be different. If the sand is loose, the volumetric strain will be contractive. On the other hand, if the sand is dense, it will dilate. A drained test defines the volumetric strain response of sand to a zero pore water pressure change condition. In other words, in order to keep the pore water pressure constant, the volume of the sand will have to change in the way as measured in a drained test. In a drained test, loose sand needs to contract, that is, to discharge water, to keep the pore water pressure constant. On the other hand, when volume change, that is, water discharge, is not allowed in an undrained test, the pore water pressure will increase. As a consequence, the effective confining stress will reduce, and the shear resistance will decrease accordingly. Static liquefaction or runaway instability will occur. Similarly, in a drained test, dense sand needs to dilate, that is, to absorb water in order to keep the pore water pressure constant. Under an undrained condition, water is not allowed to flow into the specimen, and hence the pore water pressure inside the specimen will reduce. This is why pre-failure instability does not occur in dense sand under undrained conditions. However, if a large enough dilatancy rate is imposed to force the specimen to dilate more than the sand would under a drained condition, extra water will have to flow into the specimen to generate the required dilation. As a result, positive pore water pressure will be developed. The dense specimen will become unstable under a dilatancy rate-controlled condition in a similar way to the loose sand under an undrained condition.

In a more general instability framework, the occurrence of runaway instability is affected by three main factors: (1) drainage conditions that can be simulated by the strain increment ratio imposed on the specimen ($d\varepsilon_v/d\varepsilon_1$); (2) the void ratio of the soil; and (3) the initial effective stress ratio. As discussed in detail by Chu *et al.* (1993), Chu and Leong (2001) and Wanatowski and Chu (2011), the instability condition for both loose and dense sand can be expressed by the differences between the strain increment ratio imposed during a strain path test, $(d\varepsilon_v/d\varepsilon_1)_t$, and the strain increment ratio of the soil, $(d\varepsilon_v/d\varepsilon_1)_s$, measured in a drained test.

As discussed earlier, the effect of the stress ratio on the instability behaviour of loose sand under undrained and fully drained conditions is specified by the IL shown in Figure 3(a). In recent studies, Chu *et al.* (2015) and Wanatowski and Chu (2011) demonstrated that the effective stress path obtained from a dilative strain path test on medium dense sand is very similar to that of the undrained test on loose sand. Therefore, a method similar to that under undrained and drained conditions may also be used to determine an 'IL' under dilatancy rate-controlled conditions by connecting the peak points of the effective stress paths obtained from dilative strain path tests (Chu *et al.*, 2015; Wanatowski and Chu, 2011). Such a line determined for dense sand under dilatancy-controlled conditions can be referred to as the 'peak stress line'. However, the effective stress ratio has to be sufficiently high to induce instability (Chu and Leong, 2001; Chu *et al.*, 2015; Wanatowski and Chu, 2011).

Similar to the IL determined under undrained conditions, the peak stress line determined under dilatancy rate-controlled conditions is

associated with the yield surface and defines the conditions in which large plastic yielding can take place. As such, the zone of instability can be defined for specific drainage conditions if an appropriate strain increment ratio, $d\varepsilon_v/d\varepsilon_1$, is imposed on specimens. Pre-failure instability can occur under any drainage conditions as long as the effective stress path can lead the stress state into the zone of potential instability. This behaviour is verified by the experimental data reported by Chu and Leong (2001), Chu *et al.* (2015) and Wanatowski and Chu (2011).

Conclusions

Experimental data, presented and discussed in this paper, demonstrate that dilative sand can become unstable under drainage conditions in which water infiltrates into soil mass. The factors governing the instability of dilative sand were discussed. The following conclusions can be derived from this study.

- For loose to medium dense sand, pre-failure instability in the form of a rapid and sustained increase in the axial strain rate can occur under fully drained conditions. Unlike the pre-failure instability of loose sand under undrained conditions, such pre-failure instability is not a runaway type in which the pore water pressure and the axial strain rate increase very rapidly and the soil specimen collapses almost instantly. The pre-failure stability of sand under fully drained conditions can be restored by changing the stress conditions imposed. Furthermore, the average strain rate developed in this type of instability is smaller than that developed during a runaway type of instability. To differentiate this type of instability from the runaway type, it has been called 'conditional'.
- The conditional instability occurs when a specimen is sheared along a stress path with decreasing mean effective stress and when the stress path crosses the IL.
- The slope of the IL changes with the void ratio. For loose sand, the IL determined for conditional instability is the same as that for runaway instability. For medium loose to medium dense sand, the ILs for the two types of instability are different.
- The conditional instability may provide a better explanation for failures of slopes in which the drainage condition is more appropriately assumed to be drained rather than undrained. For instance, a drawdown in water table or dredging at the toe of a slope may cause the reduction of mean stress and lead to the conditional instability.
- The pre-failure instability can occur under a dilatancy rate-controlled condition, that is, when the soil dilates. Furthermore, the conditions for the occurrence of pre-failure instability are defined based on the yielding conditions. Thus, the zone of instability can be determined regardless of the drainage conditions. The occurrence of pre-failure instability under generalised drainage conditions can be predicted using the frameworks developed by Chu *et al.* (1993, 2003) and Lade (1992, 1993) for undrained and drained conditions. Based on these frameworks, the peak

stress line can be determined by connecting the peak points of the effective stress paths determined from a series of dilative strain path tests conducted at different effective confining pressures. The validity of the peak stress line for predicting pre-failure instability of sand under dilative strain paths is verified by the experimental data reported by Chu and Leong (2001), Chu *et al.* (2015) and Wanatowski and Chu (2011).

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